### GEOMETRICAL MODELING OF WORM PROPAGATION IN CYBER-PHYSICAL SYSTEMS

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## ABSTRACT

Cyber-Physical Systems (CPS) are integral to modern infrastruc- tures, combining physical processes with computational and commu- nication capabilities. However, their complexity and interconnectivity make them vulnerable to security threats such as worm propagation. This article presents a geometrical approach to modeling worm propa- gation in CPS, providing a comprehensive framework for understand- ing the spatial dynamics of infection spread. The proposed model incorporates path and deviation equations to describe worm trajecto- ries and deviations caused by environmental factors or node mobility. Simulation results and case studies illustrate the practical application of the model, highlighting key insights and strategies for mitigating worm propagation in various CPS scenarios.

### **1 INTRODUCTION TO CYBER-PHYSICAL SYSTEMS**

Cyber-Physical Systems (CPS) integrate physical processes with computa- tional and communication elements, forming the backbone of many mod- ern technological applications. Examples of CPS include smart grids, au- tonomous vehicles, industrial automation, and intelligent transportation sys- tems [1, 2]. These systems enable real-time monitoring, control, and op- timization of physical processes through seamless interactions between the physical and digital worlds.

### **Key Components of CPS:**

**Sensors**: Devices that collect real-time data from the physical envi- ronment, such as temperature, pressure, and motion sensors. They provide critical input for computational processes.

Actuators: Devices that execute actions based on computational de- cisions, such as motors and valves, translating digital commands into physical actions.

Control Systems: Algorithms and software that process sensor data, make decisions, and generate control signals for actuators, ensuring system stability and performance.

**Communication Networks**: Infrastructure that enables data ex- change between sensors, actuators, and control systems, facilitating real-time interaction and coordination.

Computational Resources: Processing units and storage systems that analyze data, execute control algorithms, and manage system op- erations.

### **Applications of CPS**:

Smart Grids: CPS manage electricity flow, optimize energy usage, integrate renewable sources, and enhance the reliability of power dis- tribution networks.

Autonomous Vehicles: CPS enable autonomous navigation, obstacle avoidance, and interaction with traffic systems, enhancing transporta- tion safety and efficiency.

Industrial Automation: CPS control manufacturing processes, im- prove production efficiency, and support advanced techniques like robotic assembly and precision machining.

Intelligent Transportation Systems: CPS improve traffic flow, pro- vide real-time traffic information, and support smart infrastructure de- velopment.

The integration of physical and cyber components in CPS offers numerous benefits but also introduces new security challenges, particularly related to worm propagation.

### 2 CHALLENGES IN CPS SECURITY

CPS security poses unique challenges due to the integration of physical pro- cesses with cyber infrastructure. The complexity and interconnectivity of CPS make them susceptible to a range of security threats, including worm propagation [3, 4].

## Unique Security Challenges in CPS:

**Heterogeneity**: CPS consist of diverse components with varying se- curity levels, complicating the implementation of uniform security mea- sures.

**Real-Time Constraints**: CPS often operate in real-time, requiring rapid detection and mitigation of security threats without disrupting critical operations.

**Physical-Cyber Interdependence**: Attacks on the cyber compo- nents can have direct, potentially catastrophic effects on the physical processes they control.

Legacy Systems: Many CPS include older technologies with limited security features, posing integration challenges with modern security solutions.

**Scalability**: CPS can range from small systems to large-scale infras- tructures, making scalable security solutions essential.

### **Common Security Threats in CPS:**

**Worm Propagation**: Malicious software that spreads autonomously, exploiting vulnerabilities to infect nodes and disrupt operations.

Denial of Service (DoS): Attacks that overwhelm system resources, causing service disruptions or failures.

Man-in-the-Middle (MitM): Attacks where an adversary intercepts and manipulates communication between components.

**Spoofing and Tampering**: Attacks where data or control signals are forged or altered, leading to erroneous system behavior.

**Unauthorized Access**: Intrusions where attackers gain unauthorized control over system components, leading to data breaches or control hijacking.

### **Challenges in Mitigating Worm Propagation**:

**Detection**: Identifying worm activity in real-time and distinguishing it from legitimate operations.

**Containment**: Isolating infected nodes to prevent further spread with- out disrupting critical functions.

Recovery: Restoring normal operations while addressing vulnerabili- ties.

Adaptation: Developing adaptive security mechanisms to respond to evolving worm strategies.

## **3 GEOMETRICAL MODELING OF WORM PROPAGA- TION IN CPS**

Geometrical modeling provides a framework for understanding the spatial dynamics of worm propagation in CPS. By describing the paths and devia- tions of worm spread, geometrical models help identify vulnerabilities, predict infection patterns, and develop effective mitigation strategies.

### 3.1 Model Formulation

The geometrical model for worm propagation in CPS involves defining equa- tions that describe the movement of worms through the system, considering the spatial arrangement of nodes and their connections.

### **Geometrical Path Equations:**

The path of the worm is modeled using parametric equations that account for the spatial distribution of nodes and the probability of transmission be- tween them:

$$\mathbf{r}(t) = \mathbf{r}_0 + \int_0^t \mathbf{v}(\tau) \, d\tau + \mathbf{n}(t) \tag{1}$$

#### where:

 $\mathbf{r}(t)$  is the position of the worm at time t.

 $\mathbf{r}_0$  is the initial position of the worm.

 $\mathbf{v}(t)$  is the velocity vector describing the worm's movement.

 $\mathbf{n}(t)$  represents noise or deviations due to environmental factors or node mobility.

#### **Transmission Dynamics:**

The probability of transmission between nodes is influenced by their dis- tance and connectivity, described by a transmission function  $T(\mathbf{r}_i, \mathbf{r}_j)$ :

$$T(\mathbf{r}_i, \mathbf{r}_j) = \frac{\lambda}{\|\mathbf{r}_i - \mathbf{r}_j\|^{\alpha}}$$
(2)

#### where:

 $\lambda$  is a transmission coefficient.

 $\|\mathbf{r}_i - \mathbf{r}_i\|$  is the Euclidean distance between nodes *i* and *j*.

 $\alpha$  is a path-loss exponent characterizing the impact of distance on trans- mission.

#### 3.2 Path and Deviation Equations

Path and deviation equations provide a detailed description of the worm's trajectory and deviations from expected paths due to various factors.

### **Path Equation:**

The path equation describes the expected trajectory of the worm as it propagates through the CPS network:

$$\mathbf{r}_{\text{expected}}(t) = \mathbf{r}_0 + \int_0^t \mathbf{v}_{\text{expected}}(\tau) \, d\tau \tag{3}$$

where  $\mathbf{v}_{\text{expected}}(t)$  is the expected velocity vector based on initial condi-tions and network topology.

#### **Deviation Equation**:

The deviation equation describes how the worm's actual path deviates from the expected trajectory due to environmental factors or node mobility:

$$\mathbf{d}(t) = \mathbf{r}(t) - \mathbf{r}_{\text{expected}}(t) \tag{4}$$

where  $\mathbf{d}(t)$  is the deviation vector at time *t*.

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### **Impact of Deviations:**

Deviations can be caused by factors including node mobility, environ- mental changes, or interference. These deviations impact the accuracy of the worm's path prediction and the effectiveness of mitigation strategies.

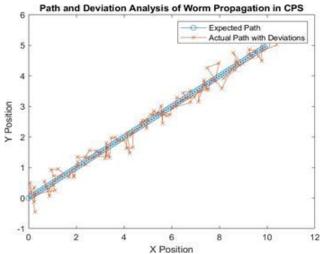


Figure 1: Path and Deviation Analysis of Worm Propagation in CPS

## **4 CASE STUDIES**

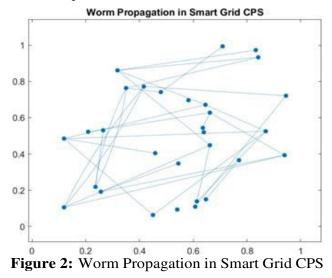
Case studies illustrate the application of geometrical modeling to real-world CPS scenarios. This section presents simulations of worm propagation in various CPS environments and analyzes the results to derive insights and develop mitigation strategies.

## 4.1 Simulation Results

Simulations are conducted to model worm propagation in different CPS sce- narios, including smart grids, industrial automation, and autonomous vehi- cles. Each simulation considers specific network configurations, node mobility patterns, and environmental factors.

### Simulation 1: Smart Grid:

In this simulation, a worm propagates through a smart grid network, targeting critical nodes such as substations and control centers. The geomet- rical model predicts the worm's path and the impact of node mobility and environmental changes on the infection spread.



## Simulation 2: Industrial Automation:

This simulation models worm propagation in an industrial automation system, focusing on how the worm spreads through interconnected machinery and control systems. The analysis includes the effects of node mobility and network topology on the worm's trajectory.

### Simulation 3: Autonomous Vehicles:

In this simulation, worm propagation is modeled in a network of au- tonomous vehicles. The geometrical model analyzes how the worm spreads

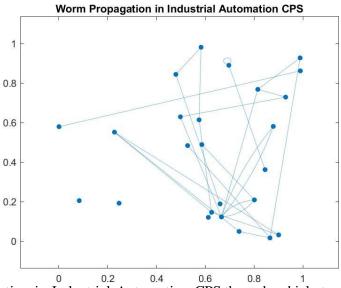


Figure 3: Worm Propagation in Industrial Automation CPS through vehicle-to-vehicle communication and the impact of mobility pat- terns on infection dynamics.

### 4.2 Analysis and Insights

The simulation results provide valuable insights into the dynamics of worm propagation in CPS and the effectiveness of geometrical modeling in predict- ing and mitigating worm spread.

### Analysis of Simulation Results:

**Smart Grid**: Highlights critical nodes and the importance of node mobility in predicting worm spread. Identifies optimal strategies for isolating infected nodes.

**Industrial Automation**: Shows how network topology and connec- tivity influence worm propagation, emphasizing the need for robust network segmentation and control mechanisms.

Autonomous Vehicles: Demonstrates the impact of vehicle mobil- ity patterns on worm spread, highlighting the importance of dynamic

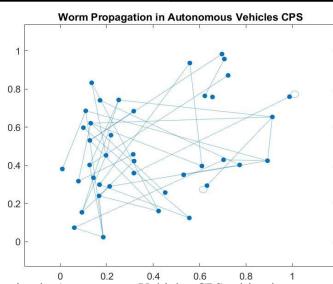


Figure 4: Worm Propagation in Autonomous Vehicles CPS mitigation strategies that adapt to changing network conditions.

## Key Insights:

Node Mobility: Significantly impacts worm propagation, affecting path predictions and mitigation strategies.

Environmental Factors: Variations in environmental conditions cause deviations from expected paths, necessitating adaptive modeling ap-proaches.

Critical Nodes: Identifying and protecting critical nodes is essential for preventing worm spread and ensuring system resilience.

**Mitigation Strategies**: Effective strategies must account for both spatial dynamics and probabilistic infection patterns to adapt to real- time network changes.

## **5** CONCLUSION

The geometrical approach to modeling worm propagation in Cyber-Physical Systems provides a comprehensive framework for understanding and pre- dicting the spatial dynamics of infection spread. By integrating geometrical insights with probabilistic analysis, the model captures both the spatial and temporal aspects of worm propagation.

The case studies demonstrate the practical application of geometrical modeling to various CPS scenarios, highlighting the importance of node mo- bility, environmental factors, and critical node protection. Future research can further enhance this approach by incorporating real-time data and adap- tive learning mechanisms to improve predictive accuracy and responsiveness to evolving threats.

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