

A Comprehensive Analysis Of The Antenna-Plasma Coupling Impedance For Icrh Heating In Tokamaks

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Abstract

In this article, the use of different matching techniques is reviewed, with particular emphasis on their function in antenna-plasma coupling impedance in the context of the Ion Cyclotron Resonance Heating (ICRH) technique for Tokamak systems. In magnetic confinement fusion studies, ICRH is a crucial method used to regulate and heat the plasma within a Tokamak. The performance and design of the antennas used to couple electromagnetic waves with the plasma are what determine how this heating method works. The study examines the body of research on helical antennas and evaluates their benefits, drawbacks, and difficulties. To emphasize the unique benefits provided by helical antennas in the context of the ICRH system on Tokamaks, comparisons with other antenna layouts are also explored. The study makes a significant contribution to our knowledge of helical antennas and how to optimize the antenna-plasma coupling impedance for ICRH performance by providing useful information about different impedance-matching approaches and procedures. The results might have a big impact on the creation of sophisticated Tokamak systems and help with the continuous attempts to achieve regulated and sustained nuclear fusion reactions.

Index Terms: Helical antennas, Ion Cyclotron Resonance Heating (ICRH), Tokamak, Impedance matching techniques, Antenna-plasma coupling, Fusion reactions.

1. INTRODUCTION

Over the decades, there has been a sharp rise in energy consumption, mirroring the population growth. Consequently, the shift towards alternative energy sources becomes a necessity. India holds the third position globally in energy consumption, trailing only China and the USA. As per the 2018 data, around 92% of the total energy consumed in India is attributed to crude oil (29.66%), coal (55.97%), and gas (6.25%), while the remaining 8% is sourced from nuclear energy, hydroelectricity, and renewable power [1]. India generates about 75% of its electricity from fossil fuels, and the resulting emission of around 10.65 billion metric tons of carbon dioxide (CO₂) annually poses a severe environmental threat, contributing to the ongoing issue of global warming. Exploring environmentally sustainable energy alternatives is imperative to meet current demands. Fusion energy stands out as a promising and secure option due to its numerous advantages [2].

1.1. FUSION ENERGY

Fusion energy liberation results from the fusion process, during which two hydrogen isotopes combine to produce helium and a neutron, releasing a substantial amount of energy [1-2]. A vast quantity of heat and gravity

characterizes the core of the sun, and it is this combination that is responsible for the process of fusion. Within controlled laboratory environments, fusion reactions have been effectively accomplished using the Tokamak apparatus, which utilizes magnetic fields to confine and regulate plasma, resulting in energy production. Deuterium gas is utilized to generate the plasma, while tritium is introduced into the plasma via pellets to initiate the fusion reaction. In the sun or stars, a fusion reaction occurs at a temperature of about 10 million degrees, facilitated by high gravitational forces. Conversely, on Earth, a fusion reactor necessitates a temperature exceeding 100 million degrees Celsius, equivalent to about 10 electron volts (eV). Achieving fusion has this as one of the prerequisites. Another requirement is maintaining an adequate density of plasma particles to ensure that a majority of collisions between nuclei take place. The third requirement involves ensuring an adequate duration of plasma confinement, which presents itself as a practical challenge. The confinement of plasma is crucial to keep it at a secure distance from the reactor, thereby averting the risk of melting [3]. Figure 1 represents a basic fusion reaction of deuterium with tritium.

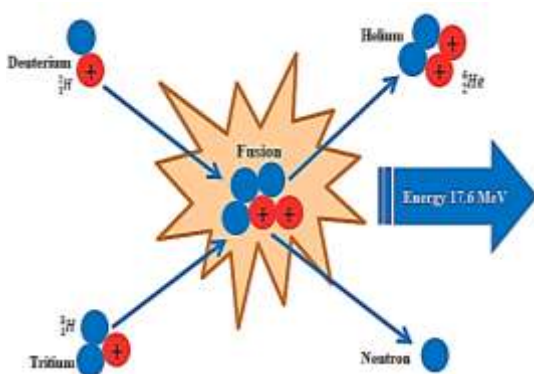


Figure 1: A basic fusion reaction of deuterium with tritium

1.2. PRODUCTION OF PLASMA AND PLASMA CONFINEMENT

The substance that forms the entirety of the universe, referred to as matter, occupies space and has mass. Existing in diverse forms like solid, liquid, and gas, matter takes on varied states. Moreover, there is another state of matter present in the universe, recognized as "the plasma state". Sir William Crookes was the first to experimentally identify the plasma state recognized as radiant matter in 1897, and the term "plasma" was coined by Irving Langmuir in 1928. The plasma state is widely acknowledged as the fourth state of matter. The ionized gas is referred to as the plasma state of matter. However, the transition from gas to plasma is not considered a thermodynamic phase transition, as it occurs gradually with rising temperature. Because of its distinctive properties that differ from fundamental states, plasma is identified as a separate state of matter, commonly recognized as the fourth state of matter. Figure 2 represents the comparison between all four states of the matter.

Similar to a gas, plasma will fill the entire volume if not confined. By employing magnetic fields, the magnetic confinement setup is tailored to confine plasma, with the inaugural selection for magnetic confinement being a linear apparatus incorporating open-field lines [4]. The formation of a torus structure, called Tokamak, occurred as a response to losses in the linear device, incorporating both toroidal and poloidal fields [3-5]. The Tokamak principle, pioneered by a Soviet physicist, remains one of the most effective designs for generating fusion power to this day. Figure 2 represents the conceptual depiction of matter transitioning into plasma.

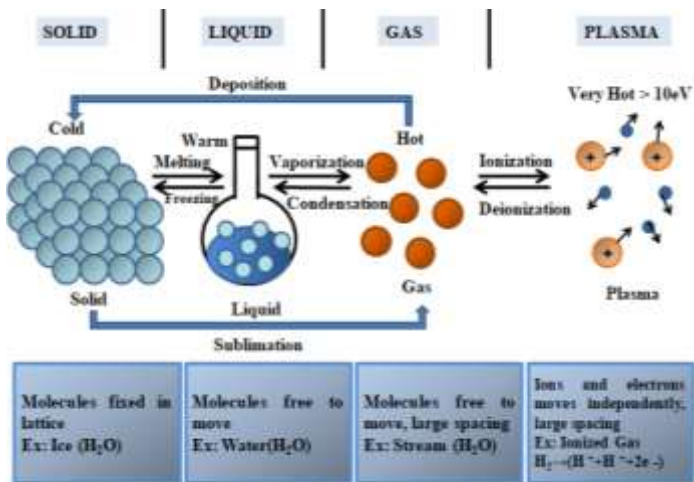


Figure 2: A conceptual depiction of matter transitioning into plasma has been illustrated.

1.3. TOKAMAK

Tokamak is a Russian word meaning large magnetic bottle. It is a device that is used to study plasma state and property. Figure 3 represents the basic diagram of tokamak.

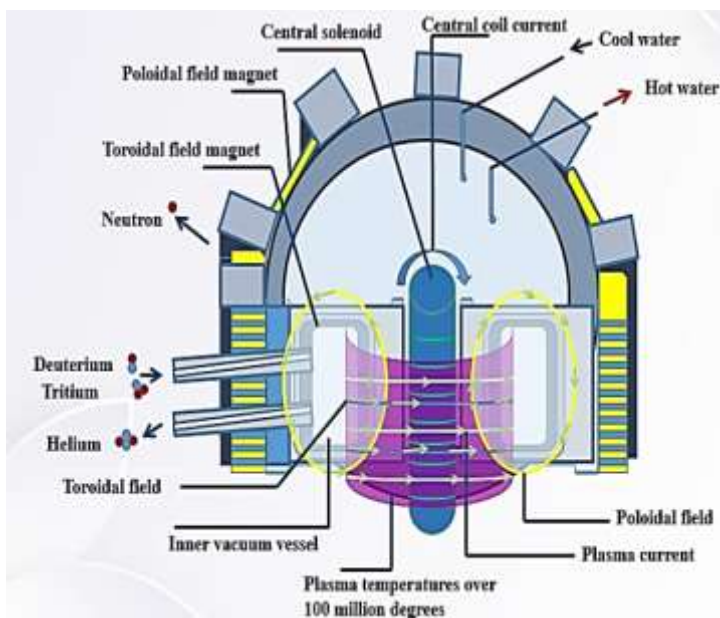


Figure 3: Tokamak- A Promising Technology for Nuclear Fusion

1.3.1. BACKGROUND

The tokamak functions as a magnetic containment device, utilized to regulate and confine high-temperature plasma, facilitating controlled fusion reactions for potential energy production [4]. Massive amounts of energy are released during the fusion process between atoms, and the exterior walls of the device collect this energy through heat. The generated heat will produce steam in the fusion power plant, which will then be converted to electricity through the use of turbines or generators.

Due to scattering, there is an energy loss, preventing the fusion process. In 1944, Enrico Fermi calculated that to maintain the fusion reaction, a self-sustaining temperature of around 50,000,000K is necessary. In the year 1945, George Paget, a British scientist, undertook several unsuccessful initiatives to develop a feasible fusion apparatus built upon the pinch effect, a method that showed potential. In the beginning, Russian physicists Sakharov and Tamm recommended refraining from the use of external magnets, as the plasma's current strength is adequate for confinement major proponents for the static toroidal setup, Golovin as well as Natan Yavlinsky, noted notable instability, such as sausage and kink instabilities, in the linear pinch notion [4]. The 'stabilized pinch' presents a further approach by creating a field outside the chamber with additional magnets before the plasma discharge. Sakharov proposed a novel approach to steady the plasma by lowering the current and employing strong outer magnets for plasma confinement. Table 1 shows a review of different tokamaks across the globe.

Table 1: An overview of well-known experimental reactors across the globe

Tokamak	Power	Frequency range	Reference
Aditya	200kW	20-47 MHz	5
SST-1	1.5MW	22.8-92 MHz	6-14
Alcator C-Mod	~6MW	40-80 MHz	15-22
ASDEX upgrade	6MW	30-120 MHz	23-27
JET	36MW	25-55 MHz	28-34
WEST	16MW	40-80 MHz	35-37
ITER	20MW/ Antenna	40-55 MHz	38-49

The first Tokamak, T-1, became operational in 1958 and exhibited notable energy losses due to impurities present in the plasma in search of a solution, the T-2 miniature device was created. The outcomes cleared the path for the development of Tokamaks around the world, including "The Culham Five" around the end of 1968, T-3, T-4, and TM-2 in 1968. Many nations began working on Tokamak development in the middle of the 1970s and by the end of the decade, several results suggested that fusion might be achieved practically—just not through a single reactor. The magnetic compression concept was put forth by Princeton Plasma Physics Laboratory (PPPL), while Oak Ridge Laboratory proposed the use of neutral beam injection. The findings from Princeton Large Torus (PLT) regarding beamforming heating lay the groundwork for a forthcoming fusion reactor. In 1979, the T-7 Tokamak achieved success with the utilization of superconducting magnets. Subsequently, other Tokamaks such as T-15, Alcator C-

mod [15-22], JT-60 [25], JET [28-34], TFTR [35], TEXTOR [37], and others followed suit. Initiated efforts on ICRH heating and conducted experiments using deuterium and tritium as fuel, revealing new challenges that constrain performance. In 1986, the USA, Japan, and the Soviet Union signed an agreement to collaborate on the construction of a larger and more potent apparatus, targeting a q factor of approximately 10. The International Thermonuclear Experimental Reactor (ITER) Association was founded as a result of this cooperative Endeavour [4]. In 2005, India formally became a part of the ITER project.

1.3.2. PLASMA HEATING

The temperature of the plasma inside the vessel is a crucial factor in the context of fusion. To facilitate a fusion reaction within the Tokamak, the plasma temperature must be sustained at around one hundred million degrees Celsius [2-3]. Attaining such elevated temperatures poses a primary challenge for scientists. Plasma is extremely responsive to electromagnetic waves and electrically conductive due to its ionized gas state. A transformer coil positioned around the vessel is used to induce a current to initiate the very first phase of plasma heating. It is also known as ohmic heating, and it works similarly to the way a heating device heats up. The quantity of heat produced inside the Tokamak is contingent on the level of electric current flowing and the plasma's resistance. Ohmic heating loses its effectiveness as the plasma temperature rises, leading to a reduction in resistance. Temperatures ranging from twenty to thirty million degrees Celsius can be reached with this heating technique. It is necessary to use a variety of heating techniques, including magnetic compression, neutral beam injection (NBI), ECRH (Electron Cyclotron Resonance Heating), ICRH, and others, to reach the optimal temperature for starting fusion [5–30]. Figure 4 Shows the schematic view of the plasma heating.

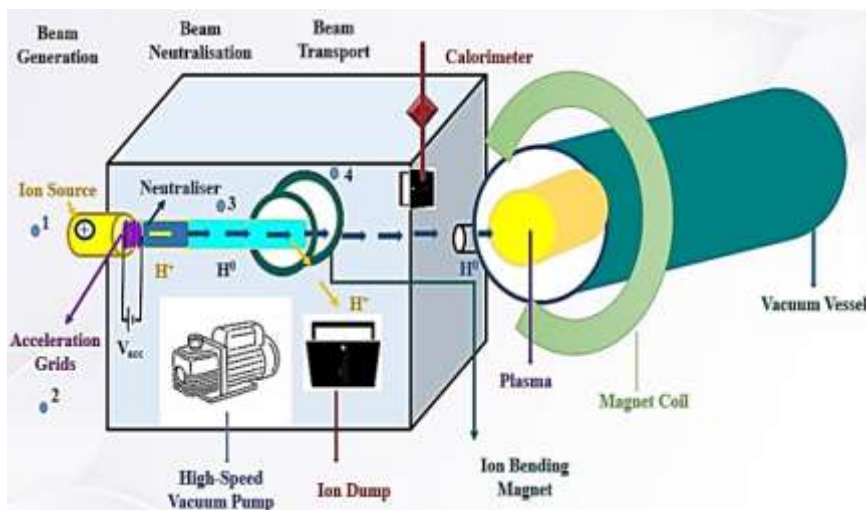


Figure 4: Schematic Diagram of Plasma Heating

- **Neutral Beam Injection (NBI)**

The high-power photon of neutral particles is introduced into the plasma via the NBI method. The plasma receives energy through coulomb interactions with the particles. The concept of NBI was initially put forth by Oak Ridge Laboratory in the mid-1970s [4, 15]. The location of ITER's initial operating NBI facility is near Padova. Although plasma heating is its primary usage, this technology is also employed in feedback management via the employment of a pulsed beam in addition to a diagnostic tool.

- **Magnetic Compression**

It is a method wherein the plasma undergoes compression through the enhancement of magnetic field confinement. The ions are compressed together, bringing them closer to one another and creating the requisite plasma density for the fusion reaction. The heating method has been utilized in the initial stages of fusion exploration. The concept of magnetic compression is still vital to the overall fusion design even though it is no longer in use.

- **Ion Cyclotron Resonance Heating (ICRH)**

Throughout recent decades, there have been continuous endeavors to explore how electromagnetic waves interact with plasma. Various fusion devices, including stellarators [15], mirror machines [4], as well as Tokamak [4-50], use the process of plasma heating via electromagnetic waves. Transmitting electromagnetic wave energy with a high frequency to the plasma is the process of Radio Frequency (RF) heating. Using RF oscillators as well as generators, the electromagnetic waves originate externally to the vessel. A rise in the motion energy of ions is the outcome result of the resonant interaction in the middle of such electromagnetic waves as well as the ionized gas. The power is subsequently passed on to other particles within the plasma through collisions, leading to the occurrence of heating.

- **Electron cyclotron resonance heating (ECRH)**

To raise the plasma temperature for fusion levels, ECRH utilizes microwave energy absorbed at frequencies corresponding to the resonance of electrons. When the incoming wave frequency aligns with that of electrons in a magnetic environment, this phenomenon occurs [15, 27]. Within the Tokamak, the frequency of the ECRH system can vary between 28 and 170 GHz, generated by specific free-electron lasers as well as gyrotron tubes.

1.3.3. OVERVIEW OF ICRH SYSTEM

India plays a pivotal role in the ITER Tokamak project, overseeing the supply of ECRH and ICRH heating systems, power supplies, and various other obligations. Within the Tokamak, the plasma is elevated to temperatures ranging in the scores of millions of degrees Celsius to attain the necessary fusion reaction rate. Employing the ICRH system for heating Tokamak plasma emerges as a promising method, particularly notable for its effectiveness in low densities as well as low magnetic fields. Moreover, the technology employed in the generation and transmission of high-power RF is comparatively cost-effective. As cited in reference [6], the ICRH setups include an RF generator, transmission conduits, a sensing unit, a tuning system, and RF antennas. The ICRH antenna receives up to megawatts of radiofrequency power to transmit power to the source via the antenna. These RF antennae then contribute to the overall plasma heating towards the fusion process by emitting radiofrequency waves within the tokamak at the plasma's ICRF frequency. Antenna impedance changes as a result of dynamic fluctuations in the plasma state around radiofrequency antennas [6-14], [38-41]. A variety of studies have provided detailed insights into the ICRH system. Below is a detailed explanation of the studies that have been carried out worldwide on the Tokamak ICRH system. These studies cover the system's structure, operating frequency range, different matching networks, detecting units, and issues that have been identified.

After the introduction, the structure of this paper involves nine sections. In section 2, an overview of the ICRH system's structure and RF transmission system on SST-1 is elaborated. Section 3 represents the review of relevant previous works. Section 4 shows the VSWR curve formulation. Non-linear least square techniques are discussed in section 5. Section 6 presents the state-of-the-art. Section 7 focuses on the conclusion. Section 8 shows the list of abbreviations.

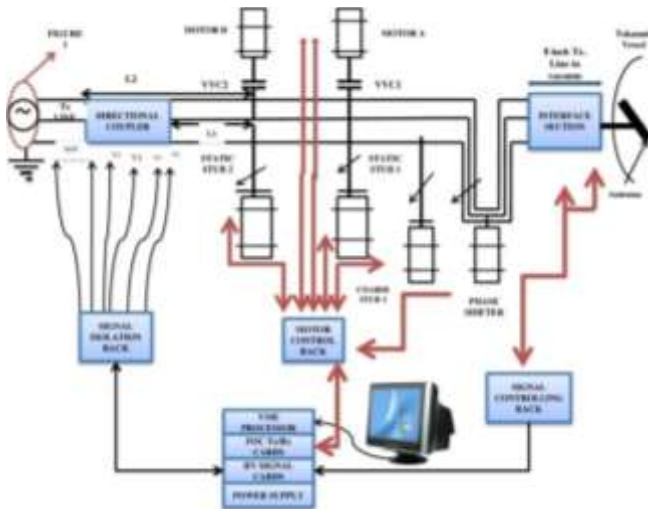


Figure 7: RF Transmission system on SST-1

2.1. Advances in Antenna-Plasma Coupling Techniques

Dynamic changes in plasma properties occur in front of RF antennae, leading to corresponding variations in antenna impedance. It is difficult to match and manage fluctuations in antenna impedance on a few millisecond time scales. Every Tokamak ICRH system has a matching system and a detecting unit to protect the system and guarantee the best possible supply of input power through the ionized gas. Figure 8 shows the diagrammatic representation of antenna-plasma coupling impedance.

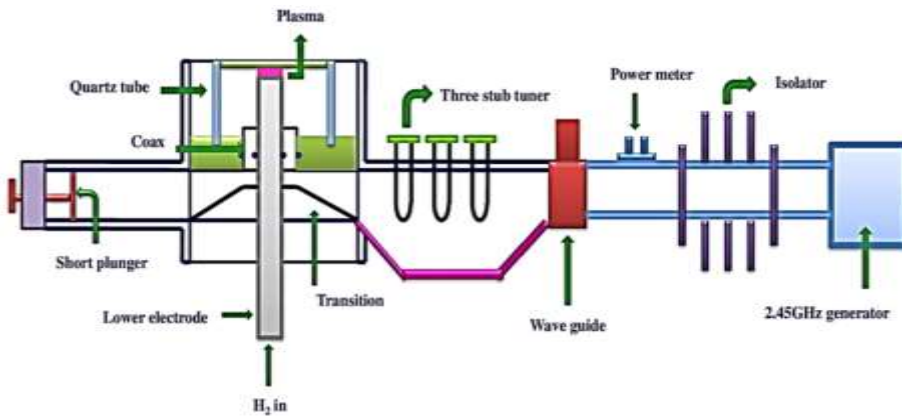


Figure 8: Diagrammatic representation of Antenna-Plasma Coupling Impedance

This section's discussion dives into a thorough examination of the matching, feedback, and detecting systems that are used in various Tokamak designs as shown in Table 2.

Table 2: Review of matching techniques used in different tokamaks

S. No.	Tokamak	Heating Method	Matching Techniques	Findings	Reference
1.	SST-1	ICRF heating	i. 3dB hybrid coupler ii. Stub tuner iii. Phase shifter	i. The power distribution for driving both antennas is achieved through the use of a 3dB hybrid coupler. ii. The VME-based data acquisition system, specifically the VERSA-Module Euro card, is integral to real-time control in the SST-1 system.	Bora et al., [6]
2.	SST-1, ITER	ICRH heating	i. 3dB hybrid coupler ii. Stub tuner iii. Phase shifter	i. Designed a 3dB hybrid coupler using strip-line technology. ii. Investigates the impact of junction disparity in high-energy settings and delves into the augmentation of frequency range through the utilization of multi-section coupled lines.	Yadav et al., [54-56]
3.	SST-1	ICRH heating	i. Stub tuner ii. Phase shifter	i. Within a brief timeframe, offline matching is executed, whereas online matching is completed in roughly 120 milliseconds.	Joshi et al., [9]
4.	JET and ASDEX	ICRH heating	i. Hybrid coupler ii. Stub tuner	i. Responding to impedance variations within a short period, the matching components exhibit different speeds, with the stub at 5 cm/sec and the trombone at 16.5 cm/sec. In JT-60 U, the trombone moves at 0.5 cm/sec, and the stub at 2 cm/sec.	Noterdaeme et al., [25]
5.	ITER	ICRH heating	i. Four hybrid couplers ii. CT junctions iii. De-coupler iv. Feedback-controlled stub	i. The modeling-derived load durability capability and antenna frequency range exhibit a striking similarity to the outcomes of the TOPICA simulation, a correspondence that holds for the ITER setup. ii. Growing the prototype dimensions to fivefold that of ITER's ICRH which involves augmenting the frequency and reducing the dimensions to one-fifth of the actual system. This alteration is implemented to examine and manage the effects of mutual interaction and fluctuations in loading.	Messiaen et al., [42]
6.	ITER	ICRH heating	i. De-coupler ii. Stub tuner iii. Phase shifters	i. Discussed the development of an algorithm utilizing an error function, accounting for both real and imaginary	Grine et al., [47]

				aspects, enabling real-time matching of impedance variations.	
7.	Alcator C-Mod	ICRH heating	i. Liquid phase shifter ii. Stub tuner	i. Stubs maintain a response time within the range of seconds, suggesting a slow operational pace.	Kumazawa et al., [55]
8.	Alcator C-Mod	ICRF system	i. Fast ferrite tuner ii. Triple stub tuner	i. Effectively match variations in real-time; nevertheless, the major drawback of the ferrite tuner lies in the pronounced RF losses resulting from biasing.	Lin et al., [19]
9.	ITER	ICRF system	i. Single Stub ii. Double stub iii. Pre-matching element iv. Faraday screen	i. A single triplet strap is employed for optimization, and the design is structured around scaled frequency parameters. ii. The antenna is accompanied by the service stub, resulting in amplified coupled power and a broadband frequency response.	P. Dumortier et al., [43]

3. REVIEW OF RELEVANT PREVIOUS WORKS

Numerous studies have been carried out on plasma within the presence of non-uniform magnetic fields in astrophysical and laboratory plasmas [18, 20]. For instance, magnetic reconnection is one of the well-known astrophysical phenomena caused by plasma flow along a non-uniform magnetic field [50]. A study of various techniques used for antenna-plasma coupling is shown in Table 3.

Table 3: A study of various techniques and outcomes is given below:

S.no.	Cited by	Favored Matching Techniques	Outcomes	Reference No.
1.	J. Staples et al.	Capacitive voltage dividers	1. Dual frequency operation has been successfully generated to get the cleanest source operation.	56.
2.	Qin Chengming et al.	Stub tuner	1. It is examined that traditional stub tuning was inferior compared to a liquid-based stub tuning method. 2. Due to the many advantageous aspects of liquid stub tuners, this has been proven to be very useful in ICRF heating experiments.	57.
3.	Pan Yaping et al.	Liquid stub tuner	1. An efficient method was used to solve the circumfluence problem. 2. The delay time is contingent upon the electromotive actuator's response time.	58.

4.	A. Girard et al.	ECR source	<ol style="list-style-type: none"> 1. An attempt has been made for the understanding of ECRIS plasma. 2. Significant development has been attained in both the field of physics and technology through multi-charged beams. 	59.
5.	D. Bora et al.	ICRH system	<ol style="list-style-type: none"> 1. The antenna impedance matching has been successfully conducted using stubs and phase shifters. 2. In the matching unit and antenna system, twenty voltage probes are being placed where VSWR is quite high. 	60.
6.	K.Saito et al.	Trial-and-error method	<ol style="list-style-type: none"> 1. The prediction was made to optimize the fluid levels and manifested the low input power of the reflection coefficient using the feedback control-based method. 2. Furthermore, there is a reduction of reflected power, and using liquid stub tuners, makes impedance matching useful for future fusion reactors. 	61.
7.	D. Bora et al.	Inductively coupled plasma chamber	<ol style="list-style-type: none"> 1. On SST-1, the ICRF system has been installed, and thorough testing has validated the functionality of all its components. 2. The launcher was thoroughly prepared for fusion on the SST-1 machine and verified for UHV compatibility. 	62.
8.	Giorgio Bacelli et al.	Double sub fast ferrite tuning system	<ol style="list-style-type: none"> 1. In terms of convergence, the Hierarchical controller showed good performance. 2. A multivariable controller has also been fabricated that observes the dependence of $\text{Im}[Z_{PL}]$ on both CL and CT. 	63.
9.	Y.Lin et al.	Triple stub fast ferrite tuning system	<ol style="list-style-type: none"> 1. On the ICRF antenna, there has been a successful implementation of a triple stub real-time FFT system. 2. The result has shown a power reflection of about 1 % in a considerable number of plasma parameters. 	64.
10.	R. Harmsworth et al.	Neutral Beam(NB) injector	<ol style="list-style-type: none"> 1. The revamped setup of the ITER beam neutralization system offers notable benefits. 2. For further computation in the adverse ion accelerator, a choice has been made in the favor of MAMuG accelerator concept, and later on, a detailed design has been verified. 	65.
11.	Raj Singh et al.	Conventional phase shifters and liquid phase shifters	<ol style="list-style-type: none"> 1. Liquid phase shifter played an important role in the Aditya tokamak. 2. At present, one phase shifter and one stub tuner are connected in Aditya Tokamak. 3. Furthermore, now two phase shifters and two stub tuners are being upgraded due to the impedance-matching network 	66.
12.	Sunil Dani et al.	Multi-limb phase shifter	<ol style="list-style-type: none"> 1. The designed parameter has been tested on this system and was also used by a fast ferrite tuner for testing the 100 kW power at the frequency range of 91.2 MHz. 	67.

13.	Dharmendra Rathi et al.	Automatic ICRH vacuum system	1. Schematics of automated vacuum systems have been established successfully in the context of raising the temperature.	68.
14.	Kishore Mishra et al.	Fast wave electron heating	1. Established the direct electron heating on tokamak Aditya with the rise in temperature of an electron with radio frequency power. 2. Significant plasma density rise has been observed due to the low impurity production.	69.
15.	H. Faugel et al.	Double stud tuners and directional coupler	1. Good measurement has been observed by installing the electricity detectors in the antenna experiencing disruptions due to the brief circuits. 2. For the cooling of the coaxial transmission line, components, and antenna are necessary for the long pulse ICRF system.	70.
16.	Gaurab Bansal et al.	Single driver negative ion source	1. An experiment has been performed on the ROBIN to test the RF-based single-driven negative ion source. 2. The extraction system has been commissioned and installation of the system is being initiated. 3. The frequency stability of the type of ferrite that is used in the matching network is still an issue.	71.
17.	Y. Lin et al.	Real-time fast ferrite tuning system	1. On the Alcator-C-mod, the plasma impedance matching has been experienced on the two traditional ports using ferrite tuners. 2. The system has attained impedance matching with the reflected power of less than 1%.	72.
18.	Raj Singh et al.	Liquid Stub Tuner	1. This study presents a novel 1–5/8” liquid stub tuner (LST) specifically designed to achieve efficient impedance matching for ion cyclotron RF signal transmission. 2. The primary aim is to enhance power transmission efficiency from the RF source to the antenna in Steady-State Superconducting and Aditya Tokamaks.	73.
19.	Dimple Yadav et al.	Automatic matching design at the center	1. An approach for designing a two-arm resistively loaded spiral antenna, as per the port constraints of SST-1 tokamak has been presented. 2. Using this technique, it becomes possible to launch electron cyclotron resonance (ECR) waves at the second harmonics with a magnetic field of 0.75T at the frequency of 284MHz.	74.

4. VSWR CURVE FORMULATION

4.1. INTRODUCTION TO PROBLEM:

ICRH has been recognized as a promising method for elevating plasma temperatures. Nevertheless, a significant challenge in ICRH lies in the coupling of RF power to the plasma. As a result of its ionized state, plasma exhibits extremely minimal resistive impedance. Therefore, ensuring alignment between the RF source impedance and the plasma impedance is imperative for ICRF heating. To achieve conformity with the plasma impedance, it is essential to first ascertain its value. In traditional approaches, the plasma impedance is determined through the utilization of the VSWR curve technique. In Aditya and SST-1, akin to tokamak devices, plasma endures for several hundred milliseconds, while the RF power supplied to the plasma amounts to a few hundred kilowatts. Within such a brief duration and with such elevated power levels, determining the VSWR curve using the sliding probe method becomes unfeasible. Therefore, the fixed probe technique is employed to ascertain plasma impedance. The voltage signal captured by the probe from the transmission line is analyzed to determine both the amplitude and phase of the reflection coefficient, thereby reducing the plasma impedance. The voltage measurements from the probe are transmitted across a distance of approximately 50 meters. Throughout this procedure, inaccuracies are introduced into the probe data. To mitigate this error, the least squares method has been applied to the voltage probe data. Additionally, under typical circumstances, a set of approximately 15 probes is employed along a span equivalent to $\lambda/2$ to ascertain the VSWR curve [75]. In this paper, a comprehensive review is provided concerning the optimal curve fitting technique aimed at reducing errors in determining both the magnitude and phase of the reflection coefficient, consequently unveiling the plasma impedance observed by the antenna.

4.2. VOLTAGE STANDING WAVE CURVE DERIVATION

The voltage distribution in a uniform two-wire transmission line under single-frequency time harmonic condition is expressed as

$$V(Z) = V_1 e^{-\gamma Z} + V_2 e^{+\gamma Z} \quad (1.1)$$

Where V_1 and V_2 are the random phasor voltages, as well as $\gamma = \alpha + j\beta$, is the wave constant. The equation of the current distribution on the line is given by

$$I(Z) = \frac{1}{Z_0} (V_1 e^{-\gamma Z} - V_2 e^{+\gamma Z}) \quad (1.2)$$

The transmission circuit is shown below in Figure 9.

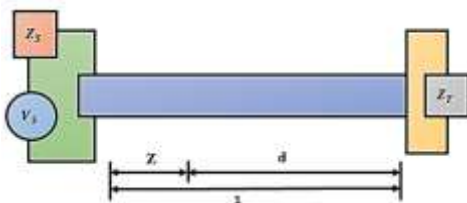


Figure 9: RF Power Flow

In this context, 1 stands for the complete length from the source to the load, with d indicating the distance from the load to a specific location along the transmission line.

The reflection coefficient at the terminal load termination is specified by

$$\rho_T = \frac{V_2 e^{+\gamma l}}{V_1 e^{-\gamma l}} = \frac{\frac{Z_r - 1}{Z_0}}{\frac{Z_r + 1}{Z_0}} \quad (1.3)$$

The equations (1.1) and (1.2) can be rewritten using $Z = l - d$

$$V(d) = V_1 e^{-\gamma(l-d)} + V_2 e^{+\gamma(l-d)} \quad (1.4)$$

$$V(d) = V_1 e^{-\gamma l + \gamma d} + V_2 e^{\gamma l - \gamma d} \quad (1.5)$$

$$V(d) = V_1 e^{-\gamma l} (e^{\gamma d} + \frac{V_2 e^{\gamma l}}{V_1 e^{\gamma l}} e^{-\gamma d}) \quad (1.6)$$

$$V(d) = V_1 e^{-\gamma l} (e^{\gamma d} + \rho_T e^{-\gamma d}) \quad (1.7)$$

As ρ_T is a complex value and can be written in terms of magnitude of reflection coefficient and phase as shown below in equation 1.8.

$$\rho_T = |\rho_T| e^{j\phi_T} = e^{-2(p+jq)} \quad (1.8)$$

Where,

$$|\rho_T| = e^{-2p} \quad (1.9)$$

$$e^{2p} = \frac{1}{|\rho_T|} \quad (1.10)$$

$$p = \ln \frac{1}{\sqrt{|\rho_T|}} \quad (1.11)$$

ρ_T is the magnitude part and will vary from 0 to 1. When ρ_T is 1 the value of p is 0 and when ρ_T is 0 or considering the value as 0.001 the value obtained of p is approximately 4 in equation no. 1.11.

$$\phi_T = -2q \quad (1.12)$$

$$q = -\frac{1}{2} \phi_T \quad (1.13)$$

The value of ϕ_T varies from $-\pi$ to π in equation 1.12 and hence q will vary from $-\pi/2$ to $+\pi/2$ in equation 1.13.

$|\rho_T| e^{j\phi_T} = e^{-2(p+jq)}$ in equation 1.8, this assumption is done to simplify the VSWR equation which can be shown below

Putting this value of ρ_T into (1.7)

$$V(d) = V_1 e^{-\gamma l} (e^{\gamma d} + e^{-2(p+jq)} e^{-\gamma d}) \quad (1.14)$$

$$V(d) = V_1 e^{-\gamma l} e^{-(p+jq)} (e^{(p+jq)} e^{\gamma d} + e^{-(p+jq)} e^{-\gamma d}) \quad (1.15)$$

Putting $e^{-(p+jq)} = \sqrt{\rho_T}$ in equation 1.15 we get,

$$V(d) = V_1 e^{-\gamma l} \sqrt{\rho_T} (e^{(p+jq)} e^{\gamma d} + e^{-(p+jq)} e^{-\gamma d}) \quad (1.16)$$

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Putting the value $\gamma = \alpha + j\beta$ in equation 1.16

$$V(d) = V_1 e^{-\gamma l} \sqrt{\rho_T} (e^{(p+jq)} e^{(\alpha+j\beta)d} + e^{-(p+jq)} e^{-(\alpha+j\beta)d}) \quad (1.17)$$

$$V(d) = V_1 e^{-\gamma l} \sqrt{\rho_T} \{e^{(ad+p)+j(\beta d+q)} + e^{-(ad+p)-j(\beta d+q)}\} \quad (1.18)$$

$$V(d) = 2V_1 e^{-\gamma l} \sqrt{\rho_T} \cosh\{(ad+p) + j(\beta d+q)\} \quad (1.19)$$

$$V(d) = 2V_1 e^{-\gamma l} \sqrt{\rho_T} [\cosh(ad+p) \cosh(j(\beta d+q)) + \sinh(ad+p) \sinh(j(\beta d+q))] \quad (1.20)$$

(where $\cosh(x+jy) = \cosh x \cos(jy) + \sinh x \sinh(jy)$), putting this in equation 1.20, we obtain

$$V(d) = 2V_1 e^{-\gamma l} \sqrt{\rho_T} [\cosh(ad+p) \cos(\beta d+q) + j \sinh(ad+p) \sin(\beta d+q)] \quad (1.21)$$

(where $\cosh(jy) = \cos x$ and $\sinh(jy) = j \sin y$)

Finding the magnitude of the standing wave in equation 1.21

$$|V(d)| = |2V_1 e^{-\gamma l} \sqrt{\rho_T}| \left\{ \cosh^2(ad+p) \cos^2(\beta d+q) + \sinh^2(ad+p) \sin^2(\beta d+q) \right\}^{\frac{1}{2}} \quad (1.22)$$

$$= |2V_1 e^{-\gamma l} \sqrt{\rho_T}| \left\{ (1 + \sinh^2(ad+p)) \cos^2(\beta d+q) + \sinh^2(ad+p) \sin^2(\beta d+q) \right\}^{\frac{1}{2}} \quad (1.23)$$

$$= |2V_1 e^{-\gamma l} \sqrt{\rho_T}| \left\{ (\cos^2(ad+p) + \sinh^2(ad+p) \cos^2(\beta d+q) + \sinh^2(ad+p) \sin^2(\beta d+q)) \right\}^{\frac{1}{2}} \quad (1.24)$$

$$= |2V_1 e^{-\gamma l} \sqrt{\rho_T}| \left\{ (\cos^2(\beta d+q) + \sinh^2(ad+p)) \right\}^{\frac{1}{2}} \quad (1.25)$$

And

$$\xi(d) = \tan^{-1}\{\tanh(ad+p) + \tan(\beta d+q)\} \quad (1.26)$$

Where $\xi(d)$ is the phase variation of the standing wave in equation 1.26.

The scaling factor $|2V_1 e^{-\gamma l} \sqrt{\rho_T}|$ is the magnitude term in equation 1.25 and can be assumed as constant. So making $|2V_1 e^{-\gamma l} \sqrt{\rho_T}|$ as a' , we get ,

$$|V(d)| = a' \left\{ \sinh^2(ad+p) + \cos^2(\beta d+q) \right\}^{\frac{1}{2}} \quad (1.27)$$

For a no-loss less $\alpha = 0$; so

$$|V(d)| = a' \left\{ \sinh^2(p) + \cos^2(\beta d+q) \right\}^{\frac{1}{2}} \quad (1.28)$$

No presumption has been taken into account in deriving this equation, thus providing VSWR curve values for various distances (d) from the terminal load[75]. In the ICRF heating experiment, frequency is of the order of a few tens of MHz and power is about 1-2 MW. In such a situation probes are fixed at certain intervals on the coaxial transmission line and voltage samples are obtained using these probes. These voltage samples are used to draw the voltage standing wave curve. There may be a possibility that these voltage samples may have errors. The source of

error may be non-uniform penetration of the probes into the transmission line. Due to unequal penetration, the voltage picked up by the probes may not be proportional to the voltage available at that point. The second source of error may be unequal attenuation of the cables used to transport the signals from voltage probes to the data acquisition rack. The third source of error may be the detectors. Detectors are used to convert RF to DC. These detectors may not give the equal value of DC for the equal value of RF power and hence introduce the error. These errors require some technique to fit a curve with minimum error with voltage probe data. In actuality, we will have voltage sample points at some fixed distance. So we need to find the parameter a, p, q that fits to discrete curve with minimum error squared. The voltage picked up by the probe is a nonlinear function of p and q, so the non-linear least square technique will be used.

5. NON-LINEAR LEAST SQUARE TECHNIQUE

The non-linear least squares methodology is a form of least squares analysis employed to match a collection of m observations with a model featuring non-linearity in n unspecified parameters (where m is greater than n) [75]. It finds utility in certain varieties of non-linear regression analysis. The fundamental principle of this approach is to estimate the model using a linear approximation and then refine the parameters through successive iterations. Numerous resemblances exist with linear least squares, yet there are also notable distinctions.

In the realm of mathematics and computing, the Levenberg-Marquardt algorithm (LMA), alternatively recognized as the damped least-squares (DLS) technique, furnishes a computational resolution to the task of minimizing a function, typically non-linear across a parameter space of the function. These minimization challenges emerge predominantly in curve fitting using least squares, where the function's dependency on the parameters is non-linear

The LMA bridges the gap between the Gauss-Newton algorithm (GNA) and the gradient descent approach. The LMA demonstrates greater resilience compared to the GNA, indicating its ability to often reach a solution even when initiated from a considerable distance away from the eventual minimum. In cases where functions behave predictably and initial parameters are sensible, the LMA typically exhibits a slightly slower pace compared to the GNA

5.1. THEORY OF GAUSS-NEWTON METHOD

The main utilization of the Levenberg-Marquardt algorithm lies in addressing the least squares curve fitting quandary, involving a collection of m observed data pairs consisting of independent and dependent variables, (x_i, y_i) , enhancing the parameters β (where β is the set of parameters) of the model curve $f(x, \beta)$ such that the total of the squares of the deviations becomes minimal.

$$F(\beta) = \sum_{i=1}^m [y_i - f(x_i, \beta)]^2 \quad (1.29)$$

The Gauss-Newton technique is an algorithm utilized to minimize the sum of the squares of the discrepancies between the data as well as the non-linear equation. The fundamental principle driving the method is the utilization of a Taylor series expansion to represent the original non-linear equation in an approximate linear format. Subsequently, the least squares method can be employed to derive fresh estimations of the parameters, aiming to diminish the residual or error. To demonstrate the procedure, initially, the association between the non-linear equation and the data can be broadly articulated as

$$y_i = f(x_i; a_0; a_1 \dots \dots a_n) \quad (1.30)$$

Where y_i = a recorded value of the outcome variable as shown in equation 1.29, $f(x_i; a_0; a_1 \dots \dots a_n)$ is a result of the independent variable x_i and nonlinear relationship of the variables $a_0, a_1 \dots \dots a_n$. For convenience, this model can be condensed by excluding the variables as

$$y_i = f(x_i, \beta) \quad (1.31)$$

Where $\beta = [a_0, a_1 \dots \dots a_n]$

Taylor series in one dimension is represented in equation 1.31

$$f(x_0 + \Delta x) = f(x_0) + \Delta x f'(x_0) + \frac{1}{2!} (\Delta x)^2 f''(x_0 + \dots) \quad (1.32)$$

The non-linear model can be elucidated using the Taylor series centered on the parameter values and truncated after the initial derivative. For instance, in a scenario involving two parameters,

$$f(x_i, \beta + \delta) \approx f(x_i, \beta) + \frac{\partial f(x_i, \beta)}{\partial a_0} \Delta a_0 + \frac{\partial f(x_i, \beta)}{\partial a_1} \Delta a_1 \quad (1.33)$$

$$f(x_i, \beta + \delta) \approx f(x_i, \beta) + J_i \delta \quad (1.34)$$

Where,

$J_i = \frac{\partial f(x_i)}{\partial \beta}$ is a gradient (row vector) of f concerning β as written in equation 1.33

At the lowest point of the sum of squares $F(\beta)$, the gradient of F to δ will be zero. The preceding primary estimation of $f(x_i, \beta + \delta)$ gives

$$F(\beta + \delta) \approx \sum_{i=1}^m (y_i - f(x_i, \beta) - J_i \delta)^2 \quad (1.35)$$

Or in vector notation,

$$F(\beta + \delta) \approx \|y - f(x, \beta) - J\delta\|^2 \quad (1.36)$$

Let's assume $y_i - f(x_i, \beta)$ in the above equation 1.35 to be Y_i for simplicity.

$$F(\beta + \delta) \approx \|Y - J\delta\|^2 \quad (1.37)$$

$$F \approx \|Y - J\delta\|^2 \quad (1.38)$$

$$F \approx (Y - J\delta)^T (Y - J\delta) \quad (1.39)$$

$$F \approx (Y^T - J^T \delta^T) (Y - J\delta) \quad (1.40)$$

$$F \approx Y^T Y - Y^T J \delta - \delta^T J^T Y + \delta^T J^T J \delta \quad (1.41)$$

$$F \approx Y^T Y - 2\delta^T J^T Y + \delta^T J^T J \delta \quad (1.42)$$

Computing the gradient of the above equation (1.41) concerning to δ we get,

$$\frac{\partial F}{\partial \delta} = \frac{\partial}{\partial \delta} (Y^T Y - 2\delta^T J^T Y + \delta^T J^T J \delta) \quad (1.43)$$

$$\frac{\partial F}{\partial \delta} = -2J^T Y + 2J^T J \delta \quad (1.44)$$

Establishing the outcome as zero yields

$$0 = -2J^T Y + 2J^T J \delta \quad (1.45)$$

$$(J^T J) \delta = J^T Y$$

By solving above equation 1.44 we get,

$$(J^T J) \delta = J^T (y_i - f(x_i, \beta)) \quad (1.46)$$

$$\delta = (J^T J)^{-1} J^T (y_i - f(x_i, \beta)) \quad (1.47)$$

Here, J denotes the Jacobian matrix where each i^{th} row is equivalent to J_i , while f and y represent the vectors containing the i^{th} component $f(x_i, \beta)$ and y_i , respectively.

Initially, the random guess is chosen as β . After that the value is calculated by solving the equation (1.3) and then the new value of the parameter is updated as $+\delta$. This equation is iterated till the value of δ is reached to the acceptable value. This algorithm is known as the Gauss-Newton Method.

Draw Back of Gauss-Newton Method

- Convergence is not guaranteed.
- The procedure might progress gradually or fail to converge entirely if the initial estimation is distant from the minimum.
- Typically, the $J^T J$ matrix is frequently either poorly conditioned or singular. To enhance and stabilize the Gauss-Newton technique for non-linear predicaments, some type of regularization becomes necessary.

5.2. THEORY OF LEVENBERG-MARQUARDT METHOD

According to the Gauss-Newton method

$$(J^T J) \delta = J^T (y_i - f(x_i, \beta)) \quad (1.48)$$

Applying damping terms to this, we get

$$(J^T J + \mu I) \delta_{lm} = g \text{ where } g = J^T (y_i - f(x_i, \beta)) \text{ and } \mu \geq 0. \quad (1.49)$$

Levenberg and Marquardt proposed employing a damped Gauss-Newton approach. The approach of adjusting the diagonal components of $J^T J$ is termed damping, and μ is denoted as the damping parameters.

The damping factor produces various impacts:

- 1) For every $\mu > 0$, the coefficient matrix is positive definite, guaranteeing that δ_{lm} constitutes a downward direction.
- 2) For high values of μ we obtain

$$\delta_{lm} \cong \frac{1}{\mu} g \quad (1.50)$$

i.e., a brief movement in the most direct descent path. This is advantageous when the current iteration is distant from the solution.

3) when μ is exceedingly diminutive, $\delta_{lm} \cong \delta_{gn}$, which presents a beneficial advancement during the concluding phases iteration, particularly when β approaches β^* , where β^* represents the actual value.

Consequently, the damping parameter impacts both the direction and magnitude of the movement, prompting the development of a technique devoid of a dedicated line search. The selection of the initial μ -value should correspond to the magnitude of the elements within $A_0 = J(\beta_0)^T J(\beta_0)$, e.g. by letting

$$\mu_0 = \tau * \max_i \{a_{ii}^{(0)}\} \quad (1.51)$$

Where τ is determined by the user. If the initial approximation is good to the true value of the parameter then $\tau = 10^{-6}$ otherwise $\tau = 10^{-3}$ or even 1. The adjustment is governed by the gain ratio.

$$\rho = \frac{F(\delta) - F(\delta + \delta_{lm})}{L(0) - L(\delta_{lm})}, \quad (1.52)$$

i.e., the ratio between the actual decrease and the predicted decrease in the function value as depicted in equation 1.51 where,

$L(0) - L(\delta_{lm}) = -2\delta_{lm}^T J^T Y \delta_{lm}^T J^T J \delta_{lm}$ as explained in equations given below from 1.52 to 1.56,

$$Y(\beta + \delta) \approx Y(\beta) + J(\beta)\delta \quad (1.53)$$

$$F(\beta + \delta) \approx L(\delta) = Y(\beta + \delta)^T Y(\beta + \delta) \quad (1.54)$$

$$= Y^T Y + 2\delta^T J^T Y + \delta^T J^T J \delta \quad (1.55)$$

$$= F(\beta) + 2\delta^T J^T Y + \delta^T J^T J \delta \quad (1.56)$$

$$F(\beta) = \sum_{i=1}^m (Y_i(\beta))^2 = \|Y(\beta)\|^2 = Y\beta^T Y(\beta) \quad (1.57)$$

Where $Y_i(\beta) = y_i - f(x_i, \beta)$ and $f(x_i, \beta)$ is a fitting model

So if the value of $\rho > 0$ then the updated damping factor μ is given by

$$\mu = \mu * \max \left\{ \frac{1}{3}, 1 - (2 * \rho - 1)^3 \right\} \quad (1.58)$$

In the above equation if lies in the range of 0 to 0.5 then the updated damping factor μ will be equal to $1 - (2 * \rho - 1)^3$. If the value of ρ is greater than 0.5 then the updated value of the damping factor will be reduced by 1/3 of the previous value.

If the value of ρ is less than zero then the damping factor μ will be double the previous value.

A substantial ρ value signifies that $L(\delta_{lm})$ closely approximates $F(\beta + \delta_{lm})$, thus allowing for its reduction to align the subsequent Levenberg-Marquardt step with the Gauss-Newton direction. If ρ is diminutive (potentially even negative), then $L(\delta_{lm})$ serves as an inadequate approximation, prompting a doubling of μ to align more closely with the steepest descent path and diminish the stride length.

The termination conditions for the algorithm ought to acknowledge that at a global minimum, we have $F'(\beta^*) = 0$, allowing for the utilization of

$$\|g\|_\alpha \leq \varepsilon_1 \quad (1.59a)$$

Where ε_1 represents a small, positive value, determined by the user. Another pertinent criterion involves halting if there's a minor alteration in δ namely,

$$\|\delta_{new} - \delta\| \leq \varepsilon_2(\|\delta\| + \varepsilon_2) \quad (1.59b)$$

This expression offers a gradual transition from a relative step size ε_2 when $\|\delta\|$ substantial absolute step size ε_2^2 if δ approaches 0. Ultimately, akin to all iterative procedures, a precaution against an endless loop is indispensable.

$$k \geq k_{max} \quad (1.59c)$$

Where ε_2 and k_{max} are chosen by the user.

6. STATE-OF-THE-ART

Whistlers refer to the low-frequency electromagnetic wave energy, typically right-circularly polarized, traversing the magnetic field within the ionosphere as well as the magnetosphere [76]. Within space research, a whistler has been specifically defined as an electromagnetic field produced by lightning that disperses as it passes through the magnetosphere and ionosphere. Sometimes referred to as "helicons," bounded whistlers are quasi-electromagnetic waves with a left- or right-hand polarization. Whistlers, on the other hand, are only electromagnetic in nature and only exhibit right-hand polarization [77]. Aigrain [78] introduced the term "helicon" in 1960 to characterize electromagnetic waves propagating within solid metal. Bowers et al. [79] were the first to observe helicon waves in metallic sodium and simultaneously examined their dispersion relation. Lehane and Thiemann [80] were the first researchers to experimentally investigate helicons in the toroidal ZETA fusion device. In their investigation of helicon wave propagation into non-uniform plasma, Blevin et al. [81] provided a qualitative explanation that clarified some of the differences in the middle of the uniform plasma theory for helicon waves and the experimental results of Lehane et al. [80]. Boswell et al. [82] pioneered the application of helicon waves in 1970 as a highly effective method for producing high-density plasma ($\sim 10^{19} \text{ m}^{-3}$). The increased interest in helicon plasma physics can be attributed to the efficient plasma production achieved through helicon waves. Plasma possessing high density and low electron (ion) temperature holds practical value as a viable source for plasma applications. Various applications benefit from the helicon source, encompassing industrial plasma processing [83, 84], pre-ionization [85, 86], current simulation for fusion systems [87–89], generation of negative ions [90, 91], and space plasma propulsion systems [92–95]. Moreover, helicon sources contribute significantly to diverse fundamental research areas, examples encompass research on dual strata, parametric deterioration instability, pressure-induced drift wave instability, and experiments with high beta. and the analysis of instability and turbulence in plasma confinement experiments. Researchers have considered a multitude of Collision and collision-less processes over the last three decades, aiming to understand their respective roles in the efficient plasma production associated with helicon waves. Chen [96] introduced the idea of Landau damping as an appropriate choice for energy transmission to the plasma. He described Landau damping as a Collisionless process where the wave power is conveyed to particles near the wave's phase velocity. Using RF-modulated emissions for Ar+ light to identify hot electrons, Molvik et al. [97] demonstrated the Landau damping associated with the wave. However, this interpretation was subsequently disproved since the experiment's fast electron count was insufficient [98]. A comparative study of various research papers has been presented in Table 4.

Table 4: Comparative assessment of matching techniques: advantages and applications.

Types of Antenna	Frequency	Favored Methodologies/Techniques	Findings	Advantages	Applications	References
Arch antenna	2.45 GHz	1. Low hybrid current drive (LHCD) 2. Left and right rectangular waveguides	i. 27 antenna elements ii. Refraction parallel index= 4.3 iii. Reflection coefficient (S_{11})= -12Db iv. Transition coefficient(S_{21})= 35 kA	i. Simple feeding ii. Low energy loss iii. High directivity	EXL-50 spherical Tokamak	99.
Spiral antenna	35-60 MHz	Electron cyclotron resonance method	i. Electron density $n_e \cong 10^{16}m^{-3}$ ii. RF power= 500W iii. RF plasma density $10^{16}V/m$ iv. Electron density of $T_e=2-6 eV$ v. Electric field of the order of $10^6V/m$ vi. Toroidal magnetic field= 3T	i. The acquired density proves to be satisfactory for achieving low loop voltage breakdown in SST-1. ii. A notable quantity of charged particles are retained within the surrounding magnetic field throughout the breakdown phase.	Steady-state superconducting tokamak (SST-1)	100.
4-turn flat spiral antenna	13.56 MHz	Helicon wave plasma discharge	i. Magnetic field= 2T ii. Electron density $=10^{12}m^{-3}$ iii. RF power= 1500W iv. Pressure= 1Pa v. Helicon wave plasma discharge vi. The density of helium plasma, approximately around $10^{12}cm^{-3}$ was assessed using a Langmuir probe.	i. A rise in the toroidal magnetic field from 0.5 to 2T led to increased uniformity within the plasma.	Experimental advanced superconducting tokamak (EAST)	101.
Traveling wave antenna	15-201 MHz	Fast wave current drive technique	i. Sharp N_z spectrum achieved ii. RF generator power is= 800kW at a frequency of 200MHz. iii. Electron temperature= 3KeV iv. Voltage standing wave ratio (VSWR)=1.35	i. Faraday shield was proposed for better antenna-plasma coupling. ii. The outer helical support is attractive, because of its compact and tight structure	JFT-2M	102.

			v. Reflected power is below 0.05%.			
Two strap antenna	25-70 MHz	ICRH system	<ul style="list-style-type: none"> i. Fed by 30Ω transmission line ii. Copper wires with a diameter of 0.5mm iii. Working frequency = 37 MHz iv. Antenna probe coupling coefficient = -54.4 dB v. Coupling coefficient= -84 dB vi. Improved antenna phasing accuracy. 	<ul style="list-style-type: none"> i. To mitigate mutual coupling between two antenna straps, a specialized decoupling mechanism was created. ii. An impedance-matching system with three tuning points was created to address the issue of impedance mismatch. iii. The creation of a directional coupler enabled the measurement of both input and reflected ICRF power. 	EAST tokamak	103.
ICRH antenna	40-70 MHz	ICRH system	<ul style="list-style-type: none"> i. Major radius= 1.75m ii. Minor radius= 0.40m iii. $B_T = 3.50$ T iv. $I_P = 1.00$ MA v. $T_{pulse} = 1000$s vi. Edge density = $N_3 = 5 \times 10^{17}m^{-3}$ 	<ul style="list-style-type: none"> i. Through numerical simulations, it is demonstrated that an appropriately chosen layout for the optimum feed location is advantageous in rendering tunable capacitors insensitive to fluctuations in the antenna input impedance when ELM plasmas occur. 	EAST-RDL (resonant double loop)	104.
ICRF antenna	35MHz	ICRF wave coupling	<ul style="list-style-type: none"> i. Major radius=$R=1.88$m ii. Minor radius=$a=0.45$m iii. Radial position of the limiter $R_0=2.34$m iv. $I_P=400\sim 500$Ka v. Toroidal magnetic field $B=2.2\sim 2.5$T vi. Frequency=34MHz vii. Total ICRF power=$0.5\sim 2$MW iii. Parallel wave no. $k_{11} =13.64$ 	<ul style="list-style-type: none"> i. Efficient methods for optimizing coupling efficiency are discussed in conjunction with the theoretical interpretation of the results. 	EAST tokamak	105.

			ix. Cut off density= $n_{\text{cutoff}}=9 \times 10^{18}/\text{m}^3$			
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7. CONCLUSIONS

The exploration of helical antennas and their impact on antenna-plasma coupling impedance in the context of ICRH for tokamak applications has revealed valuable insights into the intricacies of plasma heating mechanisms. The study has delved into the design considerations, performance characteristics, and challenges associated with spiral antennas, shedding light on their effectiveness in enhancing the efficiency of ICRH heating processes. The examination of antenna-plasma coupling impedance has offered a nuanced understanding of the complex interplay between the electromagnetic waves and the plasma medium within the tokamak environment. The state-of-the-art helicon plasmas show various techniques and the challenges of designing the parameters of various antennas to further improve their performance in tokamak scenarios. The non-linear least square technique has been also discussed in the study. Additionally, investigating novel materials and advanced technologies for antenna construction may open up new avenues for enhancing efficiency and reliability. Collaborative efforts between researchers in plasma physics, antenna engineering, and materials science will be crucial in advancing the field and overcoming existing challenges. The study serves as a foundation for future research endeavors, offering a roadmap for researchers and engineers to navigate as they strive to improve the efficacy of ICRH heating in tokamak devices. As we continue to unravel the complexities of plasma physics and antenna technologies, the prospects for achieving controlled nuclear fusion for energy production become increasingly promising.

8. LIST OF ABBREVIATIONS

SST-1	Steady state Superconducting Tokamak-1
ICRH	Ion Cyclotron Resonance Heating
RF	RF Radio frequency
ECRH	Electron cyclotron resonance heating
NBI	Neutral-beam injection
EAST	Experimental advanced superconducting tokamak
KSTAR	Korea Superconducting Tokamak Advanced Research
JT-60	Japan Torus-60
ECCD	Electron cyclotron current drive
ST	Spherical tokamak

JET	Joint European Torus
IPR	Institute for plasma research
ASDEX	Axially Symmetric Divertor Experiment
PEC	Perfect electric conductor
PLT	Princeton Large Torus
PPPL	Princeton Plasma Physics Laboratory
ORL	Oak Ridge Laboratory
ITER	International Thermonuclear Experimental Reactor
LMA	Levenberg-Marquardt algorithm
DLS	Damped least-squares
GNA	Gauss-Newton algorithm

9. DECLARATIONS:

Availability of data and materials

All the related data provided in the article.

Competing Interests

The authors declare no conflicts of interest that could influence the objectivity and impartiality of the research.

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Author's Contributions

DY have written original draft, resources, methodology, and conceptualization. VS conducted literature review. MK provided expertise in the subject matter, revised the manuscript critically for important and intellectual content. VG has done the visualization and supervision of the manuscript.

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